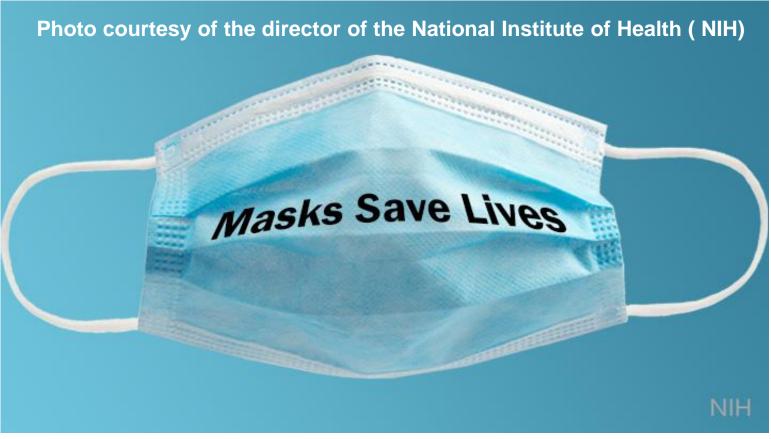
## EE 330 Lecture 28

### **Two-Port Amplifier Models**

## Exam Schedule

Exam 1 Exam 2 Exam 3 Final Friday Sept 24 Friday Oct 22 Friday Nov 19 Tues Dec 14 12:00 p.m.

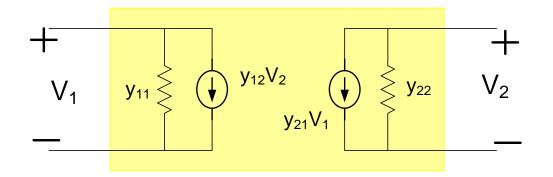


As a courtesy to fellow classmates, TAs, and the instructor

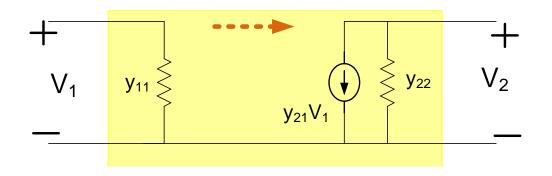
Wearing of masks during lectures and in the laboratories for this course would be appreciated irrespective of vaccination status

### Two-port representation of amplifiers

Amplifiers can be modeled as a two-port



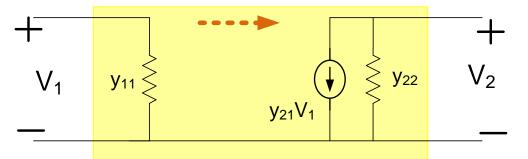
- Amplifier often unilateral (signal propagates in only one direction: wlog y<sub>12</sub>=0)
- One terminal is often common



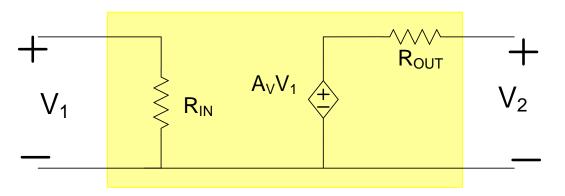
#### **Review from Previous Lecture**

### Two-port representation of amplifiers

#### **Unilateral amplifiers:**



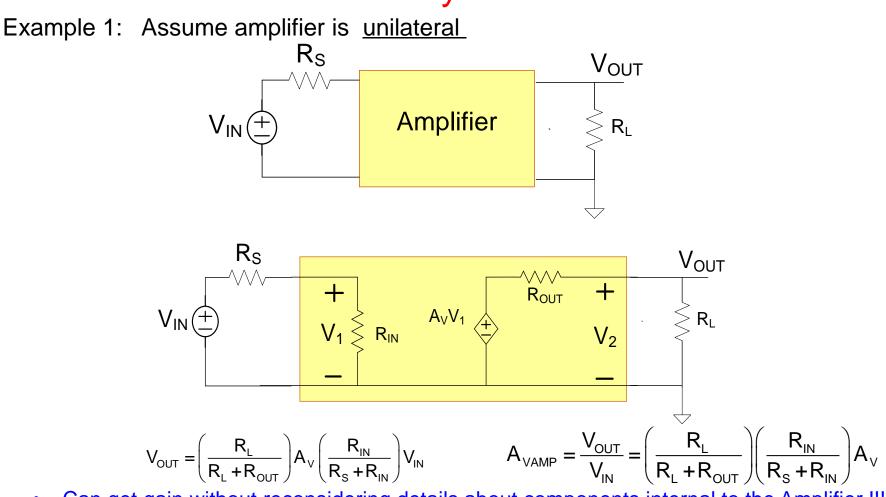
- Thevenin equivalent output port often more standard
- $R_{IN}$ ,  $A_V$ , and  $R_{OUT}$  often used to characterize the two-port of amplifiers



Unilateral amplifier in terms of "amplifier" parameters

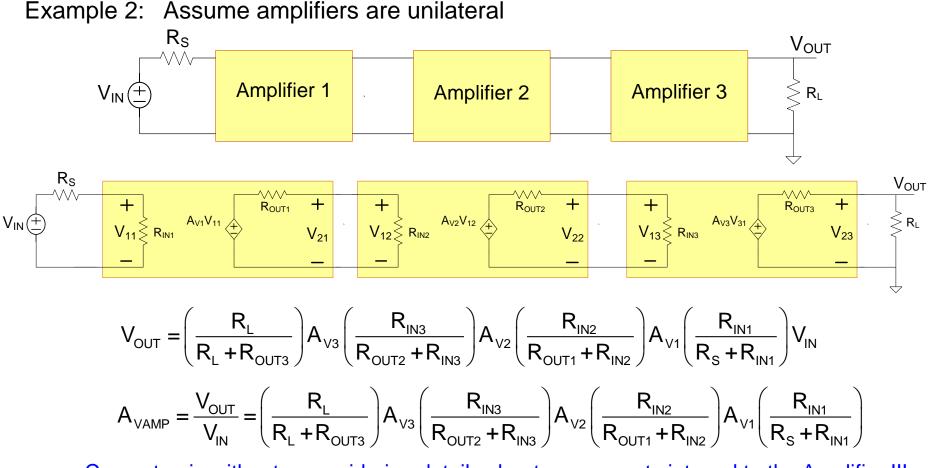
$$R_{IN} = \frac{1}{y_{11}}$$
  $A_V = -\frac{y_{21}}{y_{22}}$   $R_{OUT} = \frac{1}{y_{22}}$ 

#### Review from Previous Lecture Amplifier input impedance, output impedance and gain are usually of interest Why?



- Can get gain without reconsidering details about components internal to the Amplifier !!!
  - Analysis more involved when not unilateral

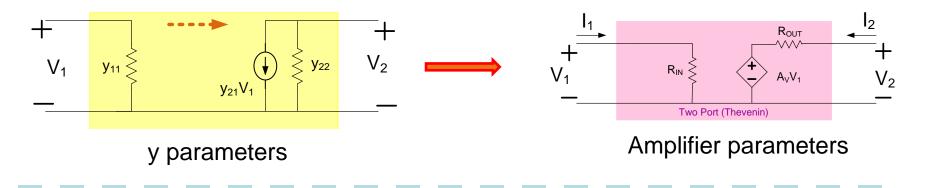
#### Review from Previous Lecture Amplifier input impedance, output impedance and gain are usually of interest Why?



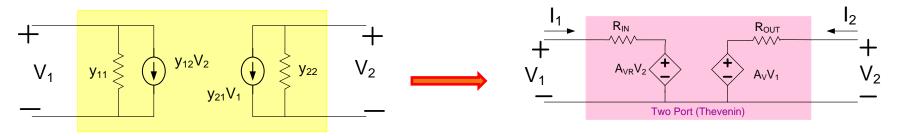
- Can get gain without reconsidering details about components internal to the Amplifier !!!
- Analysis more involved when not unilateral

### Two-port representation of amplifiers

- Amplifier often unilateral (signal propagates in only one direction: wlog y<sub>12</sub>=0)
- One terminal is often common
- "Amplifier" parameters often used



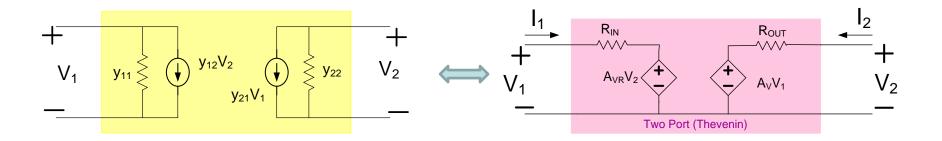
- Amplifier parameters can also be used if not unilateral
- One terminal is often common



y parameters

Amplifier parameters

#### Determination of small-signal model parameters:

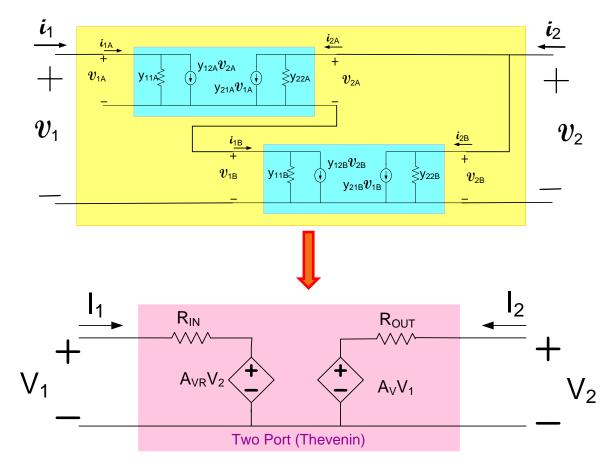


In the past, we have determined small-signal model parameters of electronic devices from the nonlinear port characteristics

- Will now determine small-signal model parameters for two-port comprised of linear networks (instead of just electronic devices)
- Could go back to the nonlinear models and analyze as we did for electronic devices
- Will follow a different approach (results are identical) that is often much easier

#### Two-Port Equivalents of Interconnected Two-ports

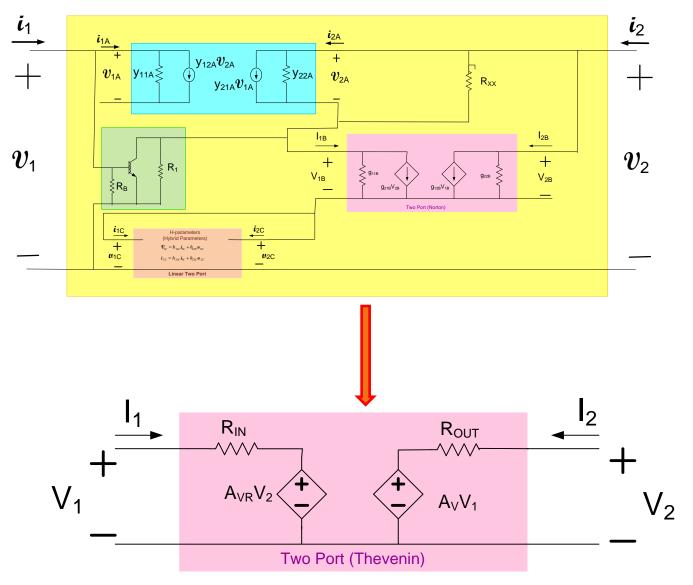
Example:



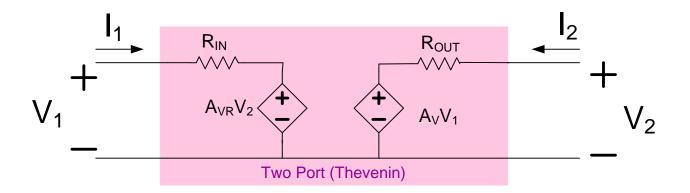
- could obtain two-port in any form
- often obtain equivalent circuit w/o identifying independent variables
- Unilateral iff  $A_{VR}=0$  (or if  $A_{V}=0$  though would probably relabel ports)
- Thevenin-Norton transformations can be made on either or both ports

#### Two-Port Equivalents of Interconnected Two-ports

Example:



#### Two-Port Equivalents of Interconnected Two-ports

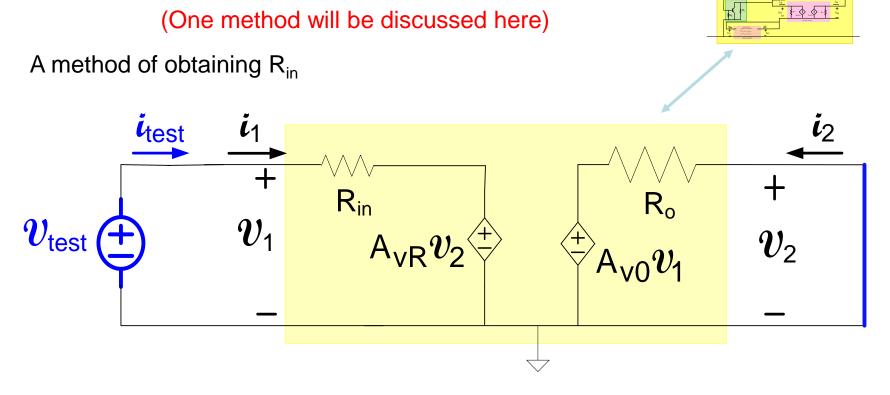


$$\boldsymbol{v}_1 = \boldsymbol{i}_1 \boldsymbol{\mathsf{R}}_{in} + \boldsymbol{\mathsf{A}}_{\mathsf{V}\mathsf{R}} \boldsymbol{v}_2$$
  
 $\boldsymbol{v}_2 = \boldsymbol{i}_2 \boldsymbol{\mathsf{R}}_0 + \boldsymbol{\mathsf{A}}_{\mathsf{V}\mathsf{0}} \boldsymbol{v}_1$ 

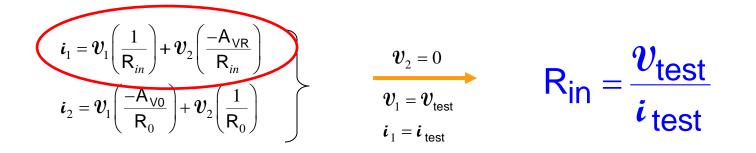
Or equivalently in form where port voltages are the independent variables

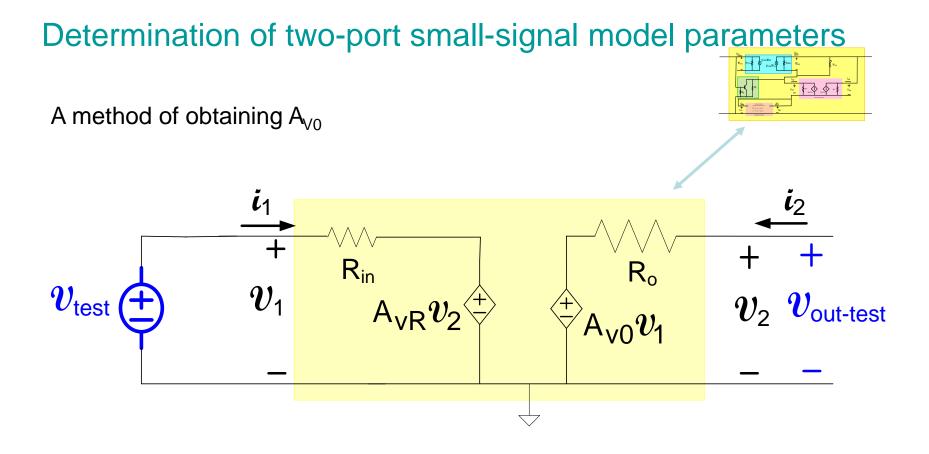
$$\boldsymbol{i}_{1} = \boldsymbol{\mathcal{V}}_{1} \left( \frac{1}{\mathsf{R}_{in}} \right) + \boldsymbol{\mathcal{V}}_{2} \left( \frac{-\mathsf{A}_{\mathsf{V}\mathsf{R}}}{\mathsf{R}_{in}} \right)$$
$$\boldsymbol{i}_{2} = \boldsymbol{\mathcal{V}}_{1} \left( \frac{-\mathsf{A}_{\mathsf{V}\mathsf{0}}}{\mathsf{R}_{0}} \right) + \boldsymbol{\mathcal{V}}_{2} \left( \frac{1}{\mathsf{R}_{0}} \right)$$

## Determination of two-port small-signal model parameters



Terminate the output in a (small signal) short-circuit





Terminate the output in a (small signal) open-circuit

$$i_{1} = v_{1} \left(\frac{1}{\mathsf{R}_{in}}\right) + v_{2} \left(\frac{-\mathsf{A}_{\mathsf{VR}}}{\mathsf{R}_{in}}\right)$$

$$i_{2} = v_{1} \left(\frac{-\mathsf{A}_{\mathsf{V0}}}{\mathsf{R}_{0}}\right) + v_{2} \left(\frac{1}{\mathsf{R}_{0}}\right)$$

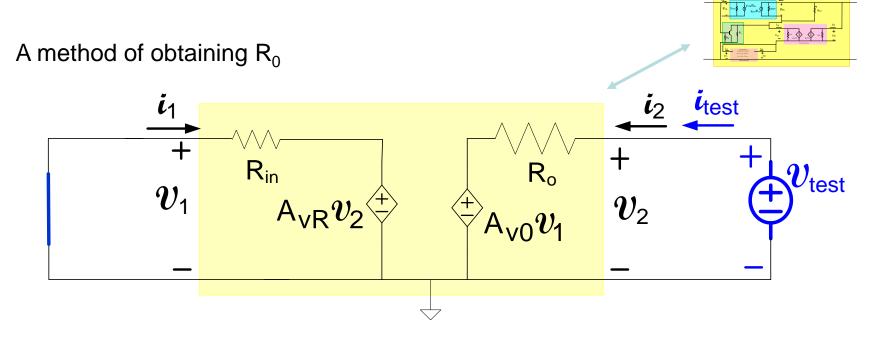
$$i_{2} = v_{\mathsf{test}}$$

$$v_{1} = v_{\mathsf{test}}$$

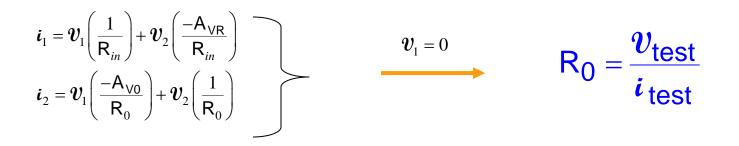
$$v_{2} = v_{\mathsf{out-test}}$$

$$\mathsf{A}_{\mathsf{VO}} = \frac{v_{\mathsf{out-test}}}{v_{\mathsf{test}}}$$

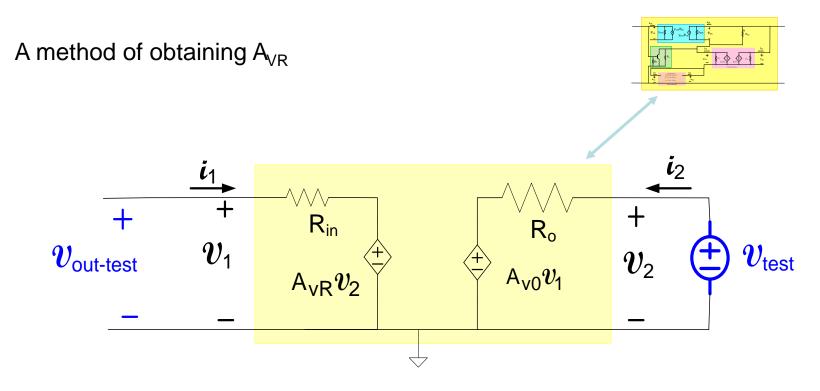
#### Determination of two-port small-signal model parameters



Terminate the input in a (small-signal) short-circuit



#### Determination of two-port small-signal model parameters



Terminate the input in a (small-signal) open-circuit

$$i_{1} = v_{1} \left(\frac{1}{\mathsf{R}_{in}}\right) - v_{2} \left(\frac{\mathsf{A}_{\mathsf{VR}}}{\mathsf{R}_{in}}\right)$$

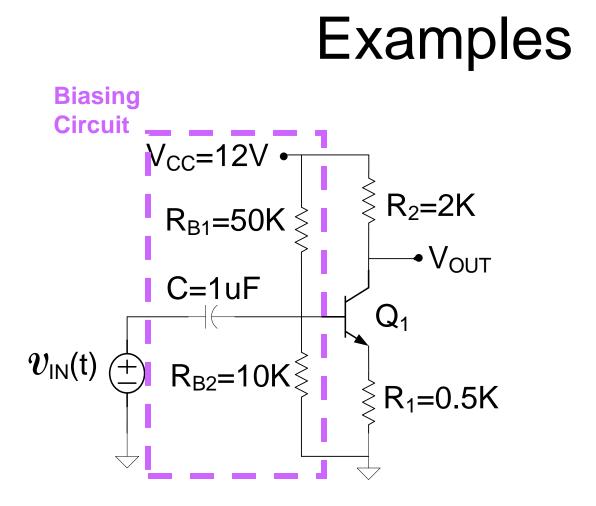
$$i_{2} = v_{1} \left(\frac{-\mathsf{A}_{\mathsf{VO}}}{\mathsf{R}_{0}}\right) + v_{2} \left(\frac{1}{\mathsf{R}_{0}}\right)$$

$$i_{1} = 0$$

$$\mathsf{A}_{\mathsf{VR}} = \frac{v_{\mathsf{out-test}}}{v_{\mathsf{test}}}$$

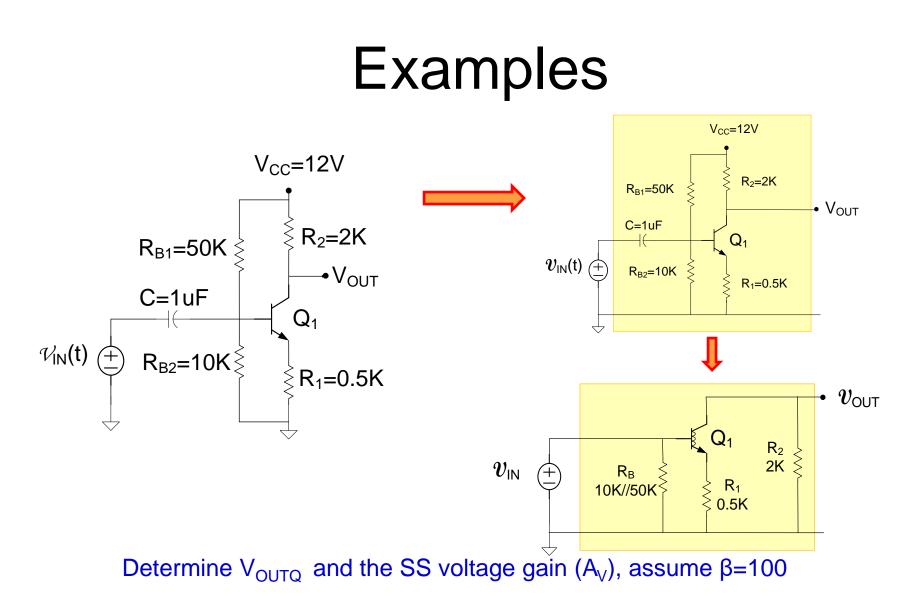
#### **Determination of Amplifier Two-Port Parameters**

- Input and output parameters are obtained in exactly the same way, only distinction is in the notation used for the ports.
- Methods given for obtaining amplifier parameters  $R_{in}$ ,  $R_{OUT}$  and  $A_V$  for unilateral networks are a special case of the non-unilateral analysis by observing that  $A_{VR}$ =0.
- In some cases, other methods for obtaining the amplifier parameters are easier than the " $V_{\text{TEST}}$ :  $I_{\text{TEST}}$ " method that was just discussed



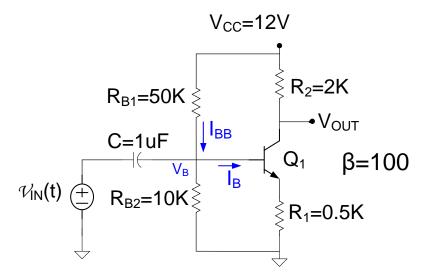
Determine V<sub>OUTQ</sub> and the SS voltage gain (A<sub>V</sub>), assume  $\beta$ =100

(A<sub>V</sub> is one of the small-signal model parameters for this circuit)

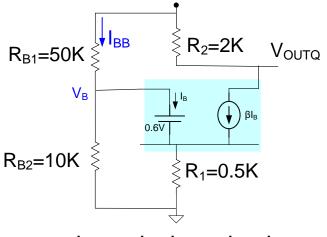


(A<sub>v</sub> is one of the small-signal model parameters for this circuit)

### Examples



### Determine V<sub>OUTQ</sub> V<sub>cc</sub>=12V



dc equivalent circuit

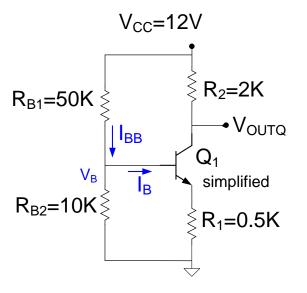
This circuit is most practical when  $I_B << I_{BB}$ With this assumption,

$$V_{B} = \left(\frac{R_{B2}}{R_{B1} + R_{B2}}\right) 12V$$

$$C_{CQ} = I_{EQ} = \left(\frac{V_{B} - 0.6V}{R_{1}}\right) = \frac{1.4V}{.5K} = 2.8mA$$

$$V_{OUTQ} = 12V - I_{CQ}R_{1} = 6.4V$$

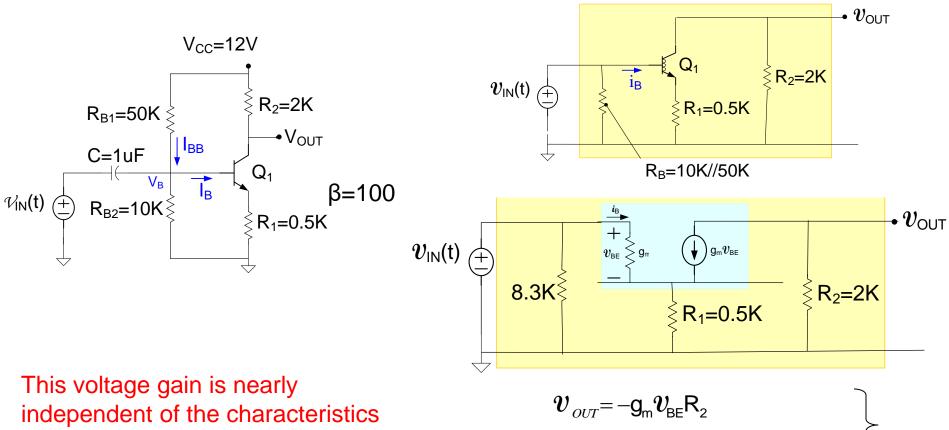
Note: This Q-point is nearly independent of the characteristics of the nonlinear BJT !



dc equivalent circuit

### Examples

#### Determine SS voltage gain



of the nonlinear BJT !

This is a fundamentally different amplifier structure

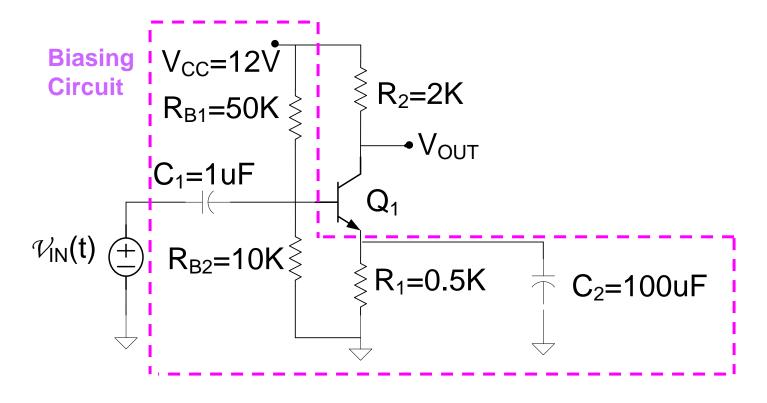
It can be shown that this is slightly non-unilateral

$$v_{OUT} = -g_m v_{BE} R_2$$

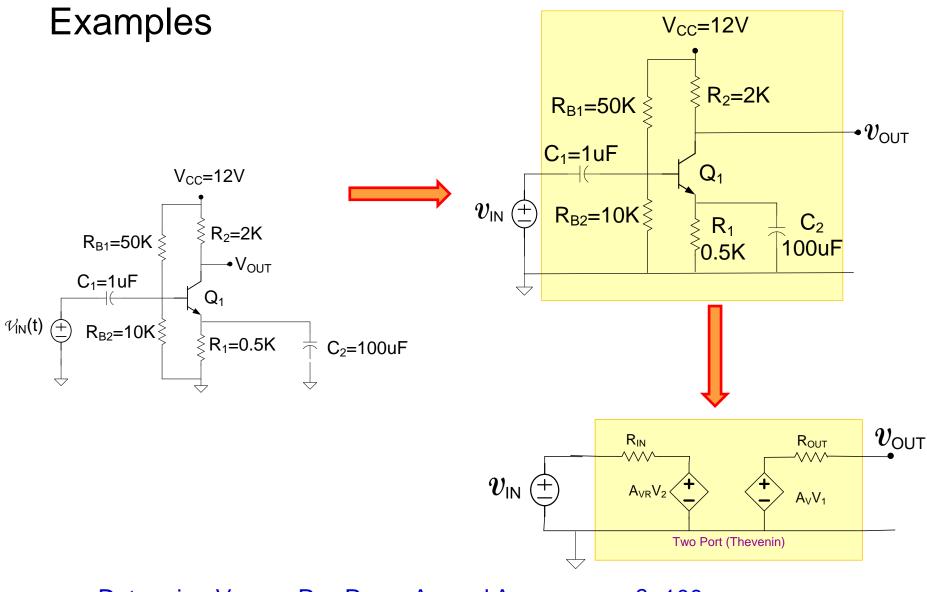
$$v_{IN} = v_{BE} + R_1 (v_{BE} [g_\pi + g_m])$$

$$A_{V} = \frac{-R_{2}g_{m}v_{BE}}{v_{BE} + R_{1}(v_{BE}[g_{\pi} + g_{m}])} = \frac{-R_{2}g_{m}}{1 + R_{1}([g_{\pi} + g_{m}])}$$
$$A_{V} \cong \frac{-R_{2}g_{m}}{R_{1}g_{m}} = \frac{-R_{2}}{R_{1}} = -4$$





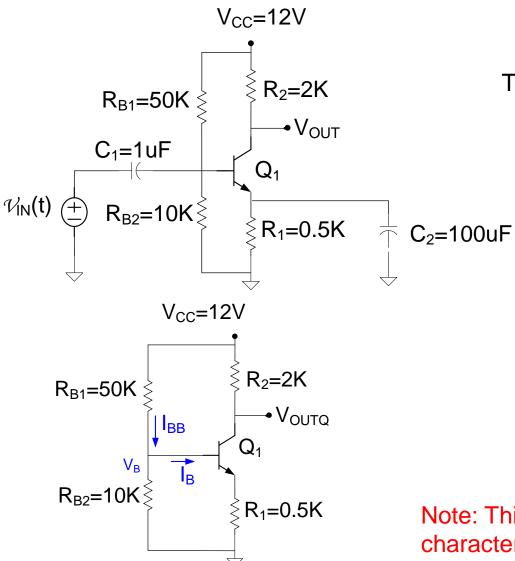
Determine  $V_{OUTQ}$ ,  $R_{IN}$ ,  $R_{OUT}$ , and the SS voltage gain, and  $A_{VR}$  assume  $\beta$ =100



Determine  $V_{OUTQ}$ ,  $R_{IN}$ ,  $R_{OUT}$ ,  $A_V$ , and  $A_{VR}$ ; assume  $\beta$ =100

 $(A_V, R_{IN}, R_{OUT}, and A_{VR}$  are the small-signal model parameters for this circuit)

#### Examples



Determine V<sub>OUTQ</sub>

This is the same as the previous circuit !

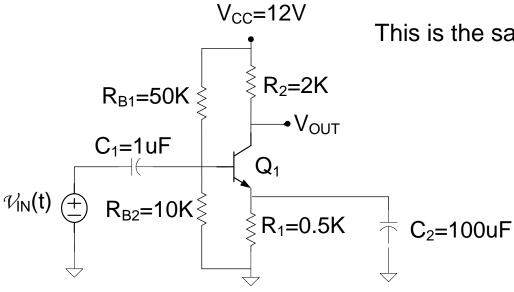
$$V_{OUTQ} = 6.4V$$

$$_{CQ} = \frac{5.6V}{2K} = 2.8mA$$

Note: This Q-point is nearly independent of the characteristics of the nonlinear BJT !

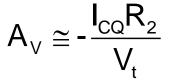
The dc equivalent circuit

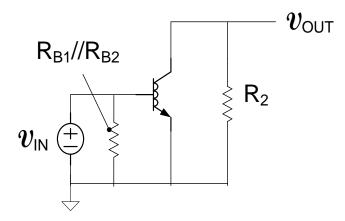
#### Examples Determine the SS voltage gain A<sub>V</sub>



This is the same as another previous-previous circuit !

$$A_{v} \cong -g_{m}R_{2}$$





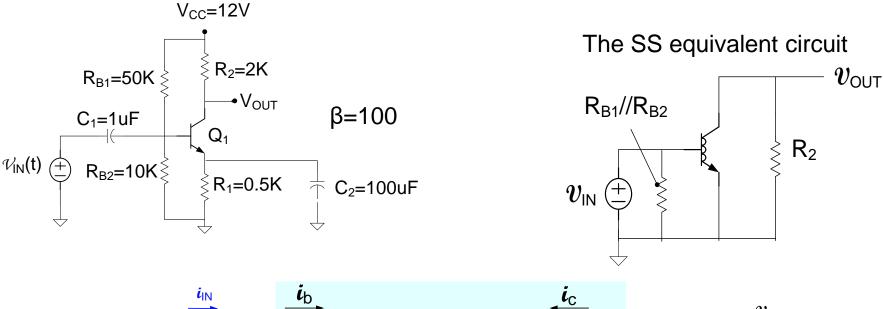
$$A_{\rm V} \cong -\frac{5.6\rm V}{26\rm mV} = -215$$

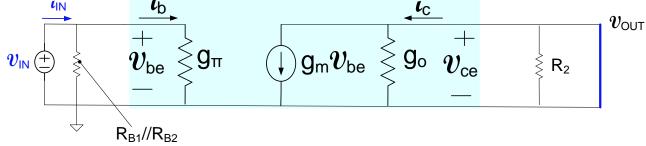
Note: This Gain is nearly independent of the characteristics of the nonlinear BJT !

The SS equivalent circuit



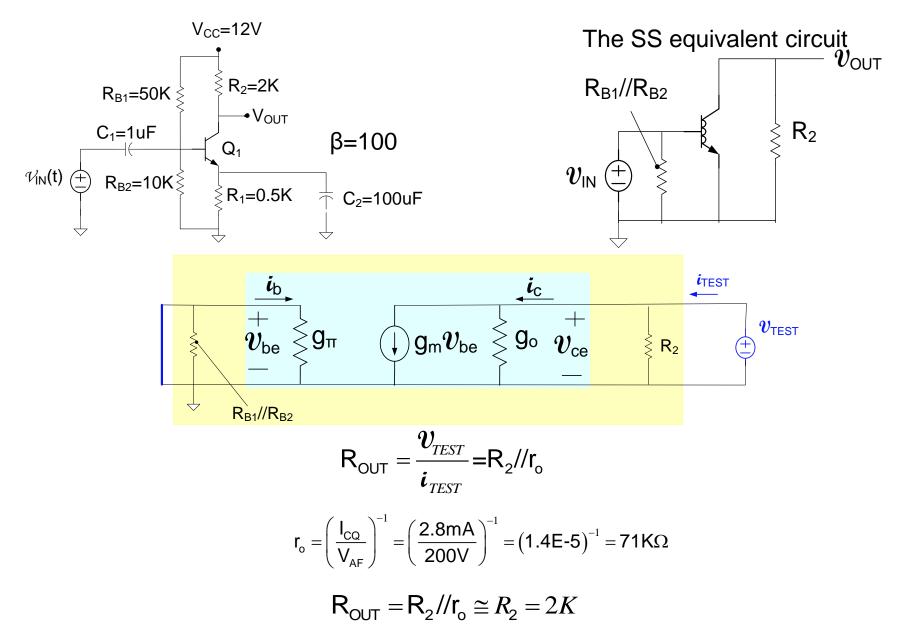
#### Determination of R<sub>IN</sub>



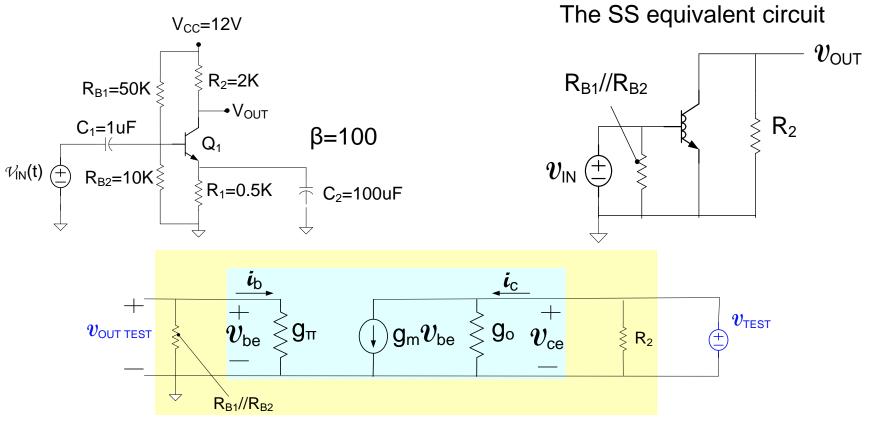


 $R_{IN} = R_{B1} / / R_{B2} / / r_{\pi} \cong r_{\pi}$  $r_{\pi} = \left(\frac{I_{CQ}}{\beta V_{t}}\right)^{-1} = \left(\frac{2.8 \text{mA}}{100 \bullet 26 \text{mV}}\right)^{-1} = 928\Omega$  $R_{IN} = R_{B1} / / R_{B2} / / r_{\pi} \cong r_{\pi} = 930\Omega$ 

#### Examples Determination of R<sub>OUT</sub>



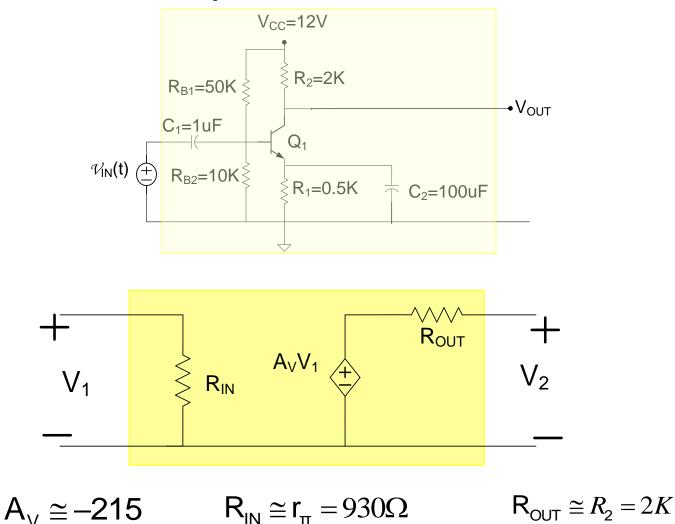
#### Examples Determine A<sub>VR</sub>



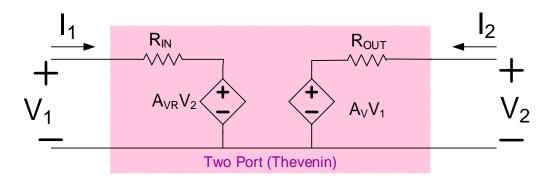
$$v_{_{OUT\,TEST}}$$
=0

$$A_{VR} = 0$$

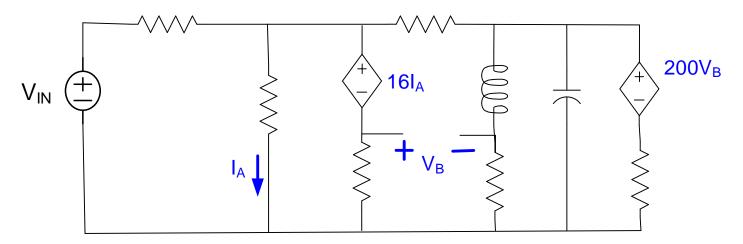
# Determination of small-signal two-port representation



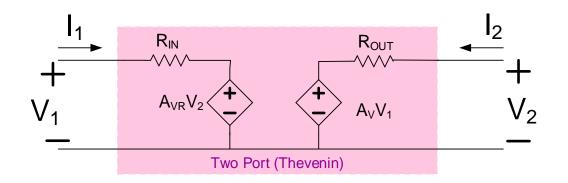
This is the same basic amplifier that was considered many times



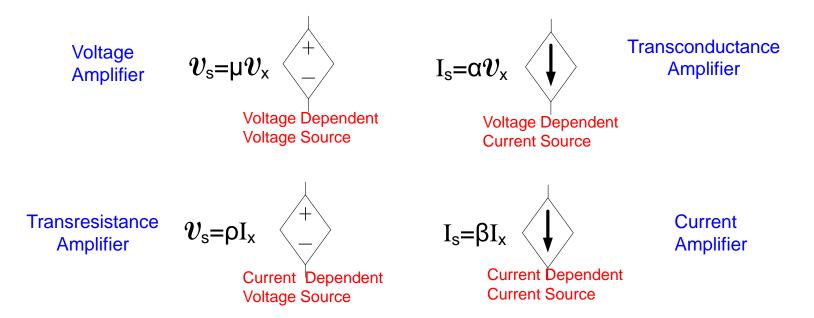
Dependent sources from EE 201

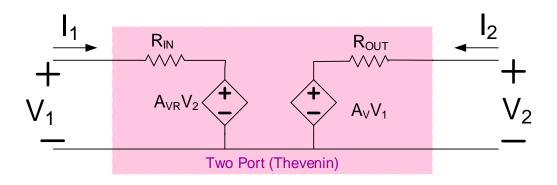


Example showing two dependent sources

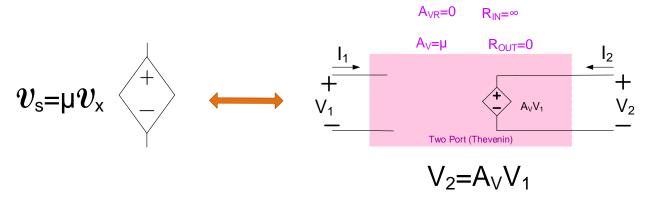


Dependent sources from EE 201

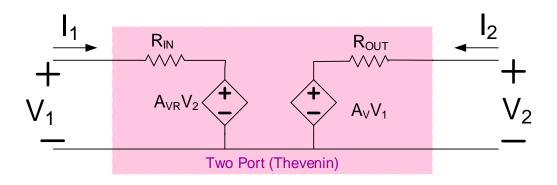




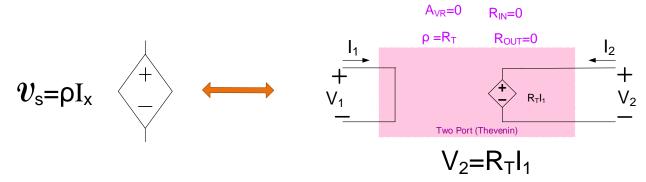
It follows that



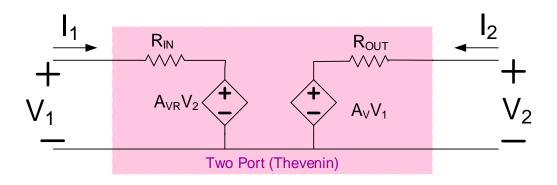
Voltage dependent voltage source is a unilateral floating two-port voltage amplifier with  $R_{IN} = \infty$  and  $R_{OUT} = 0$ 



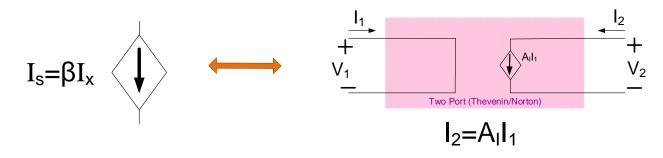
It follows that



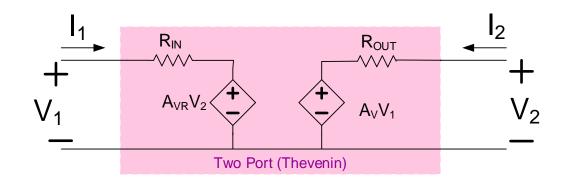
Current dependent voltage source is a unilateral floating two-port transresistance amplifier with  $R_{IN}=0$  and  $R_{OUT}=0$ 

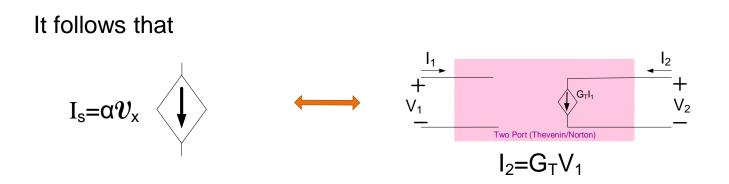


It follows that



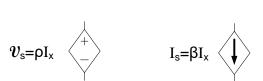
Current dependent current source is a floating unilateral two-port current amplifier with  $R_{IN}$ =0 and  $R_{OUT}$ = $\infty$ 





Voltage dependent current source is a floating unilateral two-port transconductance amplifier with  $R_{IN} = \infty$  and  $R_{OUT} = \infty$ 

### Dependent Sources $v_{s=\mu}v_x \stackrel{\downarrow}{\swarrow}_{I_s=\alpha}v_x \stackrel{\downarrow}{\downarrow}$



Dependent sources are unilateral two-port amplifiers with ideal input and output impedances

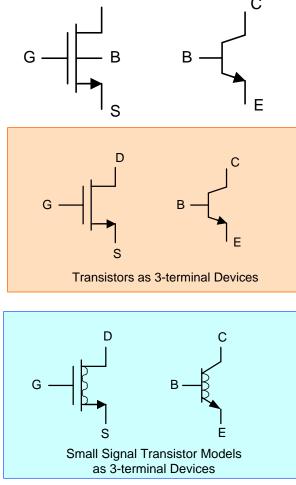
Dependent sources do not exist as basic circuit elements but amplifiers can be designed to perform approximately like a dependent source

- Practical dependent sources typically are not floating on input or output
- One terminal is usually grounded
- Input and output impedances of realistic structures are usually not ideal

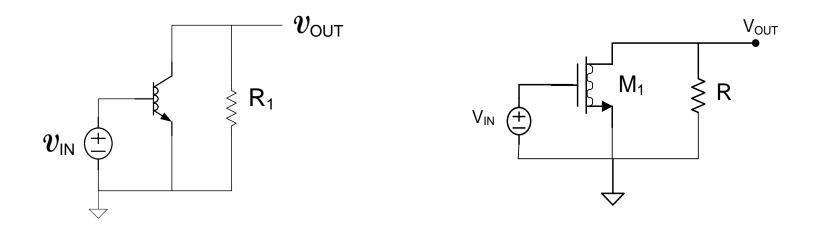
Why were "dependent sources" introduced as basic circuit elements instead of two-port amplifiers in the basic circuits courses???

Why was the concept of "dependent sources" not discussed in the basic electronics courses???

- MOS and Bipolar Transistors both have 3 primary terminals
- MOS transistor has a fourth terminal that is generally considered a parasitic terminal

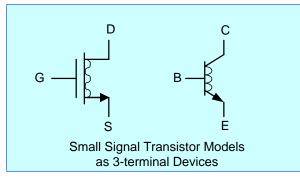


Observation:



These circuits considered previously have a terminal (emitter or source) common to the input and output in the small-signal equivalent circuit

For BJT, E is common, input on B, output on CTermed "Common Emitter"For MOSFET, S is common, input on G, output on DTermed "Common Source"

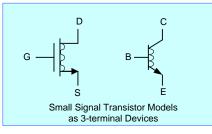


Amplifiers using these devices generally have one terminal common and use remaining terminals as input and output

Since devices are nearly unilateral, designation of input and output terminals is uniquely determined

Three different ways to designate the common terminal

Source or Emitter	termed Common Source or Common Emitter
Gate or Base	termed Common Gate or Common Base
Drain or Collector	termed Common Drain or Common Collector



**Common Source or Common Emitter** 

**Common Gate or Common Base** 

**Common Drain or Common Collector** 

MOS		BJT			
ommon	Input	Output	Common	Input	Output
S	G	D	E	В	С
G	S	D	В	Е	С
D	G	S	С	В	E

Identification of Input and Output Terminals is not arbitrary

It will be shown that all 3 of the basic amplifiers are useful !



## Stay Safe and Stay Healthy !

## End of Lecture 28